

EE 3350

MATLAB INTRODUCTION

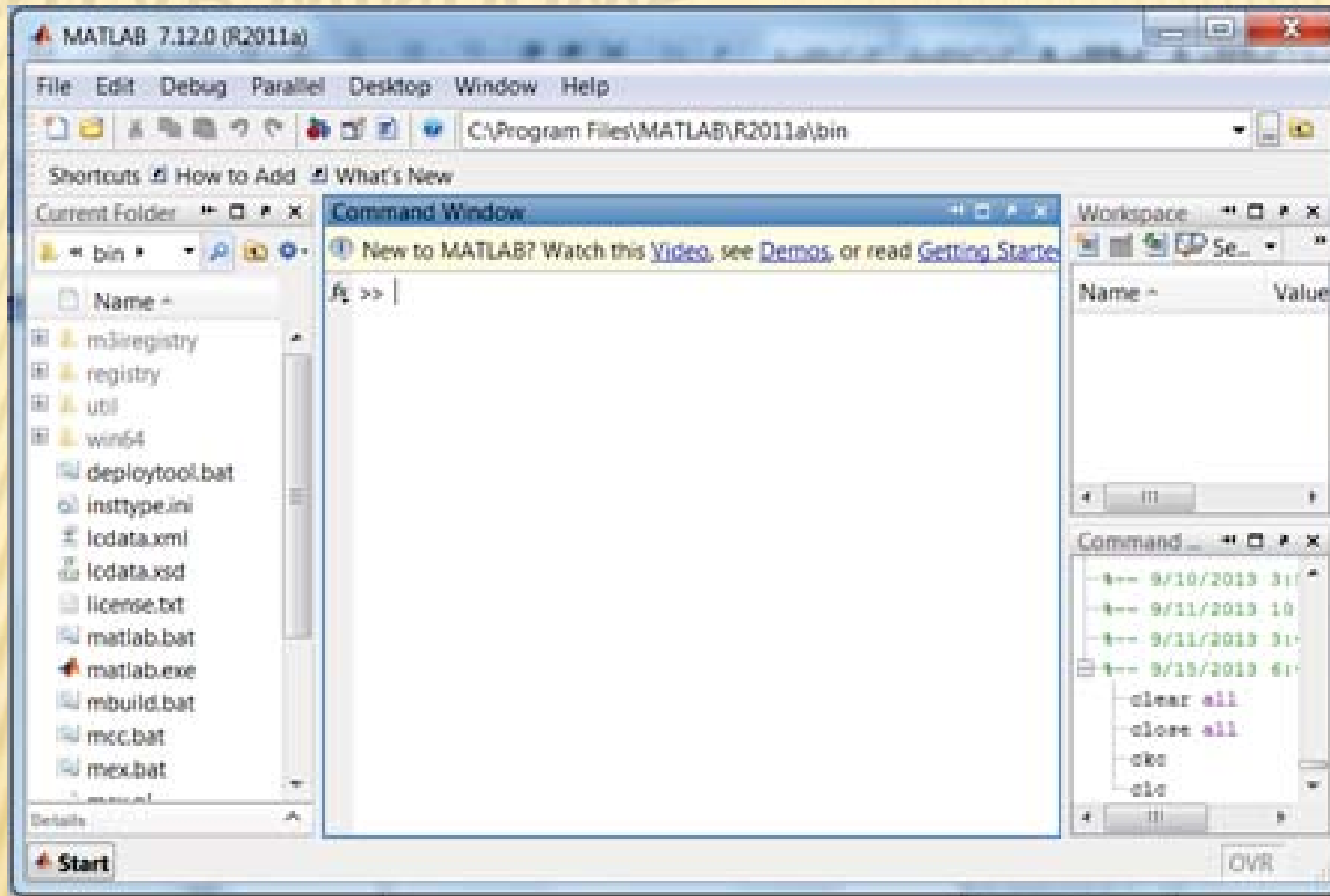
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WHAT IS MATLAB?

- MATLAB is a numerical computing environment developed by MathWorks.
- MATLAB allows matrix manipulations, plotting of functions and data, and implementation of algorithms.
- MatLab program and script files always have filenames ending with ".m".
- The programming language is exceptionally straightforward since almost every data object is assumed to be an array.

MATLAB WINDOWS



- We can type the commands in the command window.
- As for programming, .m file script is preferred.
File → New → Script

GETTING HELP

- ✘ Online help is available from the Matlab prompt (a double arrow)

- ✘ **generally** (listing all available commands):

```
>> help
```

[a long list of help topics follows]

- ✘ **specific commands:**

```
>> help fft
```

[a help message on the fft function follows].

DATA REPRESENTATIONS IN MATLAB

- ✘ **Variables:** Variables are defined as the assignment operator “=” . The syntax of variable assignment is
variable name = a value (or an expression)
- ✘ **Example:**

```
>> x = 5
x =
    5
>> y = [3*7, pi/3];
```

DATA REPRESENTATIONS IN MATLAB

- ✘ **Vectors/Matrices** : MATLAB can create and manipulate arrays of 1 (vectors) , 2 (matrices), or more dimensions.
- ✘ row vectors: $a = [1, 2, 3, 4]$ is a 1X4 matrix
- ✘ column vectors: $b = [5; 6; 7; 8; 9]$ is a 5X1 matrix
- ✘ Example:

```
>> A = [1 2 3; 7 8 9; 4 5 6]
A      =
     1     2     3
     7     8     9
     4     5     6
```

ARITHMETIC OPERATIONS

- ✘ Five basic arithmetic operators

Symbol	Description	Example
+	addition	$3.3+8.5$
-	subtraction	$5.2-3$
*	multiplication	$3*4$
/	division	$8/2$
^	power	2^3

ARITHMETIC OPERATIONS

- ✘ Three operators working on an element-by-element basis.

Symbol	Description	Example
.*	multiplication of two vectors, element-wise	3.*4
./	division of two vectors, element-wise	8./2
.^	raising all the elements of a vector to a power	2.^3

The results of the three examples are the same as those of * / ^. But what will happen when it comes to the vector operations?

VECTOR OPERATIONS

Consider the vectors:

$$\mathbf{x} = [x_1, x_2, \dots, x_n]$$
$$\mathbf{y} = [y_1, y_2, \dots, y_n]$$

The following operations indicate the resulting vectors:

$$\mathbf{x} \cdot^* \mathbf{y} = [x_1 y_1, x_2 y_2, \dots, x_n y_n]$$

$$\mathbf{x} \cdot / \mathbf{y} = \left[\frac{x_1}{y_1}, \frac{x_2}{y_2}, \dots, \frac{x_n}{y_n} \right]$$

$$\mathbf{x} \cdot \wedge^p = [x_1^p, x_2^p, \dots, x_n^p]$$

VECTOR OPERATIONS

Examples:

(1) Compute the dot product: $\sum_i x_i y_i$

```
>> x=[2,1,4];  
>> y=[3,5,7];  
>> x*y'
```

```
ans =
```

```
39
```

(2) Compute an element-by-element multiplication of two vectors:

```
>> x=[2,1,4];  
>> y=[3,5,7];  
>> x.*y
```

```
ans =
```

```
6    5    28
```

RELATIONAL & LOGICAL OPERATORS

Relational Operators

Symbol	Description
\leq	less than or equal
$<$	less than
\geq	greater than or equal
$>$	greater than
$==$	equal
\neq	not equal

Logical Operators

Symbol	Description
$\&\&$	AND
$\ \ $	OR
\sim	NOT

CONTROL FLOW

.m files have the following control flow constructs:

- × if statements
- × for loops
- × while loops

Each of the constructs needs to terminate with an end statement.

CONTROL FLOW

if: conditional execution of certain parts of a code

Example:

Matlab code:

```
x=-1;  
if x>0  
    str='positive';  
elseif x<0  
    str='negative';  
elseif x==0  
    str='zero';  
else  
    str='error';  
end
```

Results: **negative**

CONTROL FLOW

for : repeat certain commands in a predetermined way

Example:

Matlab code:

```
x=0;  
for i=1:3  
    x=x+i;  
end
```

Results: 6

CONTROL FLOW

while: repeats a sequence of commands as long as some condition is met.

Example:

Matlab code:

```
x=-3;
while x<0
    disp('one more time!');
    x=x+1;
end
```

Results:

```
one more time!
one more time!
one more time!
```

MATHEMATICAL FUNCTIONS IN MATLAB

- ✘ MATLAB offers many predefined mathematical functions for technical computing, e.g.

<code>cos(x)</code>	Cosine	<code>abs(x)</code>	Absolute value
<code>sin(x)</code>	Sine	<code>angle(x)</code>	Phase angle
<code>exp(x)</code>	Exponential	<code>conj(x)</code>	Complex conjugate
<code>sqrt(x)</code>	Square root	<code>log(x)</code>	Natural logarithm

- ✘ Colon operator (:)

Suppose we want to enter a vector x consisting of points $(0, 0.1, 0.2, 0.3, \dots, 5)$. We can use the command

```
>> x = 0:0.1:5;
```


FFT FUNCTION IN MATLAB

✘ fft function uses the Fast Fourier transform algorithm to compute Discrete Fourier transform.

✘ **Syntax**

$$Y = \text{fft}(x)$$

$$Y = \text{fft}(x, n)$$

✘ **Definition**

The functions $Y = \text{fft}(x)$ and $y = \text{ifft}(X)$ implement the transform and inverse transform pair given for vectors of length N by:

$$X(k) = \sum_{j=1}^N x(j) \omega_N^{(j-1)(k-1)}$$

$$x(j) = (1/N) \sum_{k=1}^N X(k) \omega_N^{-(j-1)(k-1)}$$

$$\omega_N = e^{(-2\pi i)/N}$$

Is an Nth root of unity

FFT FUNCTION IN MATLAB

× Description

$Y = \text{fft}(x)$ returns the DFT of vector x , computed with a fast Fourier transform algorithm.

$Y = \text{fft}(x, n)$ returns the n -point DFT. If the length of x is less than n , x is padded with trailing zeros to length n . If the length of x is greater than n , the sequence x is truncated.

BASIC PLOTTING IN MATLAB

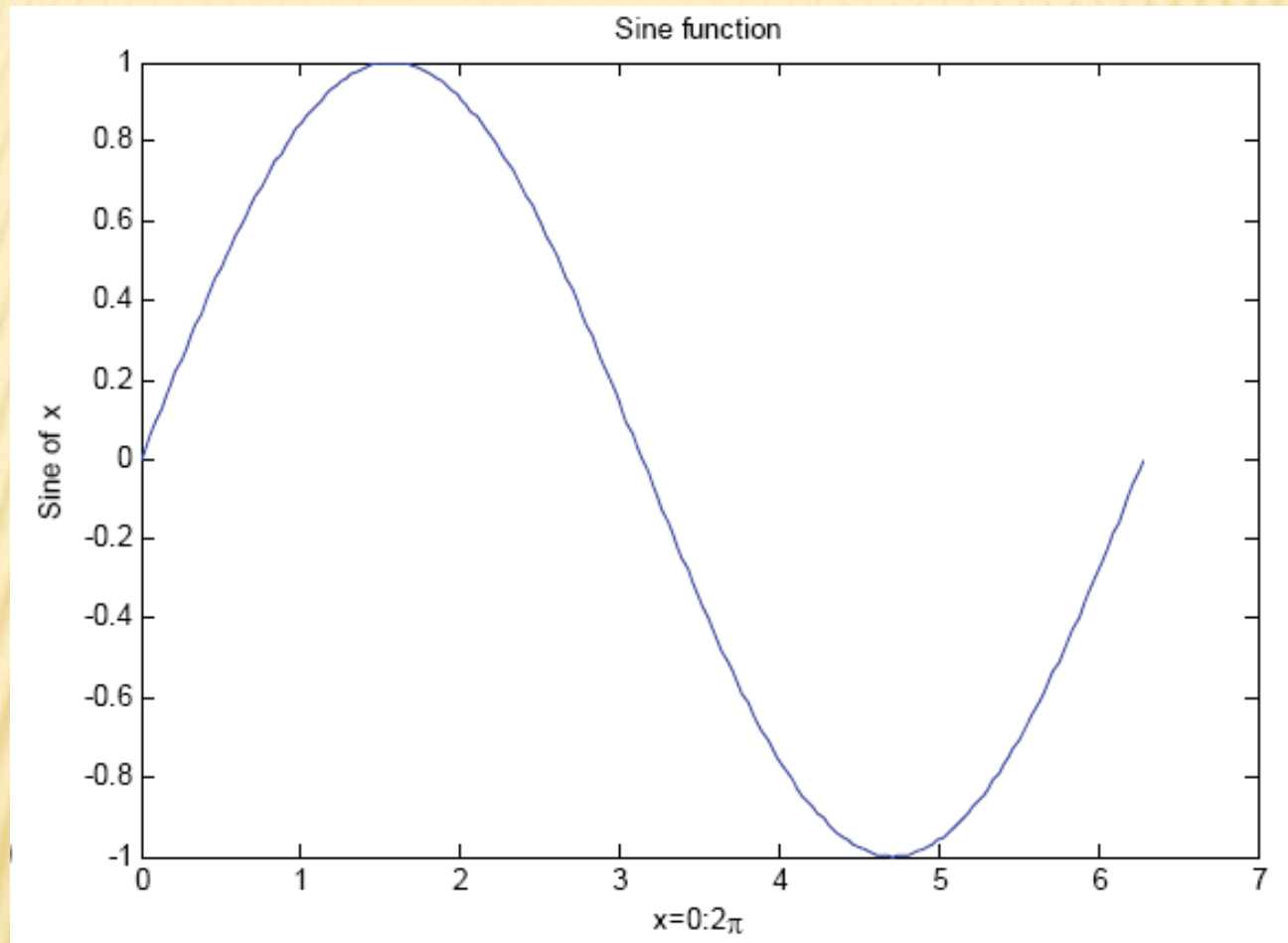
- ✘ MATLAB has an excellent set of graphic tools. Plotting a given data set or the results of computation is possible with very few commands .
- ✘ The MATLAB command to plot a graph is `plot(x,y)`, e.g.

```
>> x = 0:pi/100:2*pi;  
>> y = sin(x);  
>> plot(x,y);
```

- ✘ MATLAB enables you to add axis labels and titles, e.g.

```
>> xlabel('x=0:2\pi');  
>> ylabel('Sine of x');  
>> title('Sine function');
```

BASIC PLOTTING IN MATLAB



BASIC PLOTTING IN MATLAB

Example 1: Sine Wave

Matlab code:

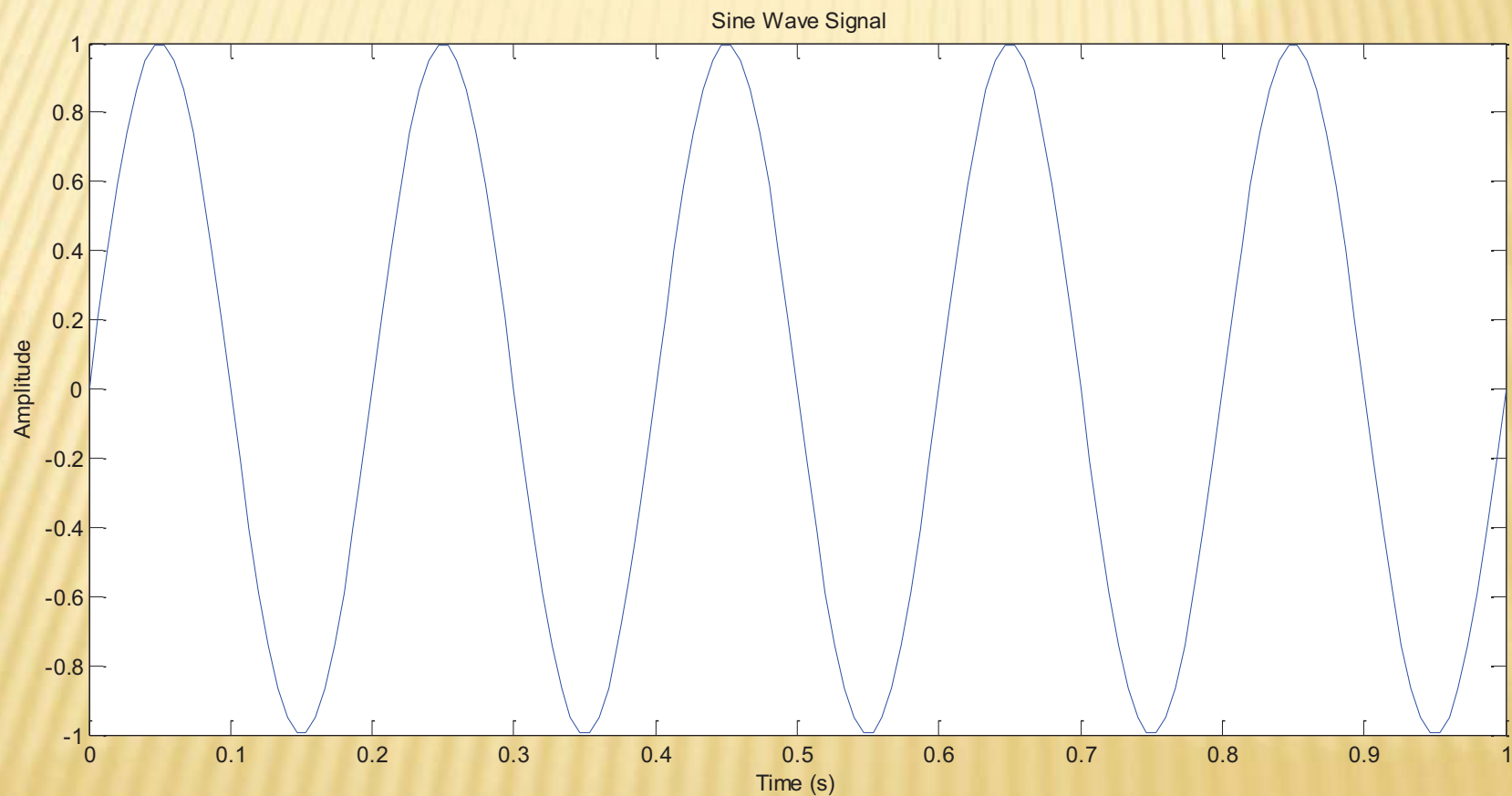
```
Fs = 150; % Sampling frequency
t = 0:1/Fs:1; % Time vector of 1 second
f = 5; % Create a sine wave of f Hz.
x = sin(2* pi*f*t);
% Take fft
% fftshift places the frequency samples in
% the right order
X = fftshift(fft(x));
% Take the magnitude of fft of x
X_mag = abs(X);
% Frequency vector
df=-Fs/2:1:Fs/2;
```

```
% Generate the plot, title and labels
figure(1);
plot(t,x);
title('Sine Wave Signal');
xlabel('Time (s)');
ylabel('Amplitude');
figure(2);
plot(df,X_mag);
title('Spectrum of a Sine Wave');
xlabel('Frequency (Hz)');
ylabel('Amplitude');
```

BASIC PLOTTING IN MATLAB

Example 1: Sine Wave

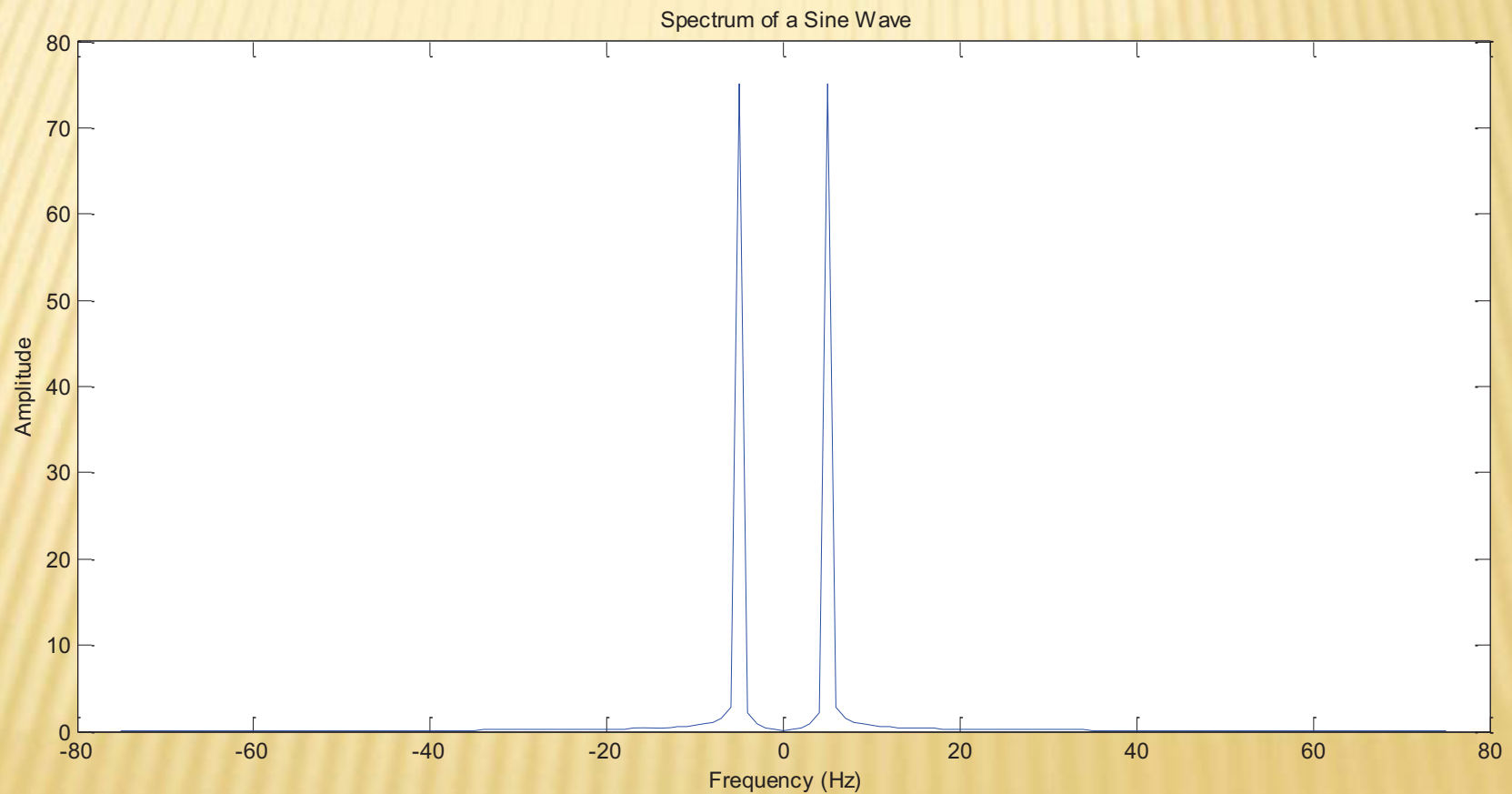
Plot: signal in time domain



BASIC PLOTTING IN MATLAB

Example 1: Sine Wave

Plot: signal in frequency domain



BASIC PLOTTING IN MATLAB

Example 2: Multiplication of two Cosine Waves

Matlab code:

```
f1 = 20; f2=10
```

```
Fs = 200; % Sampling frequency
t = 0:1/Fs:1; % Time vector of 1 second
f1 = 20; % Create a sine wave of f Hz.
f2 = 10;
x = cos(2* pi*f1*t).*cos(2* pi*f2*t);
% Take fft
% fftshift places the frequency samples in
% the right order
X = fftshift(fft(x));
% Take the magnitude of fft of x
X_mag = abs(X);
% Frequency vector
df=-Fs/2:1:Fs/2;
```

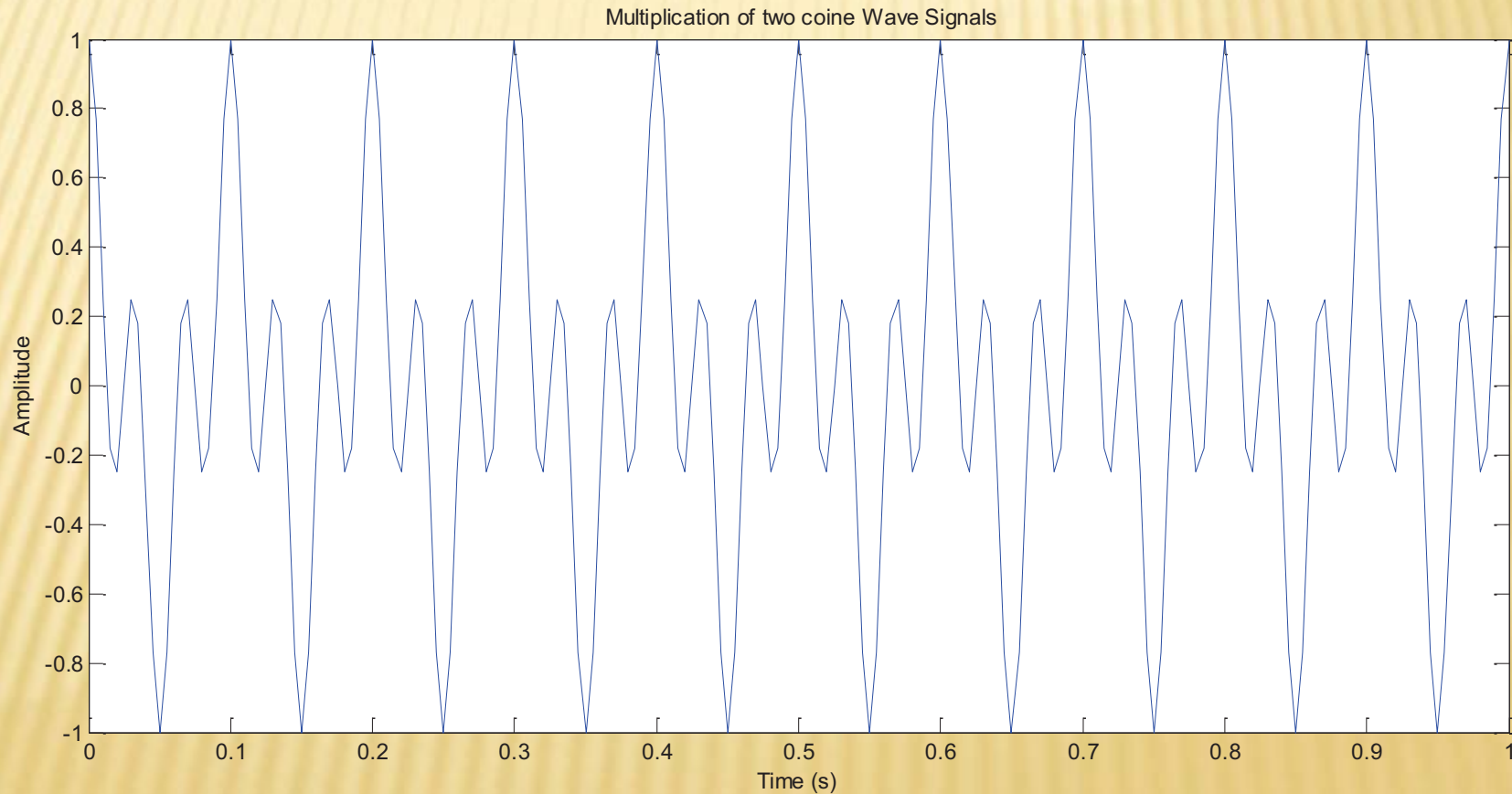
```
% Generate the plot, title and labels
figure(1);
plot(t,x);
title('Multiplication of two coine Wave Signals');
xlabel('Time (s)');
ylabel('Amplitude');
figure(2);
plot(df,X_mag);
title('Spectrum of a Sine Wave');
xlabel('Frequency (Hz)');
ylabel('Amplitude');
```


BASIC PLOTTING IN MATLAB

Example 2: Multiplication of two Cosine Waves

Plot: signal in time domain

$f_1 = 20$; $f_2 = 10$

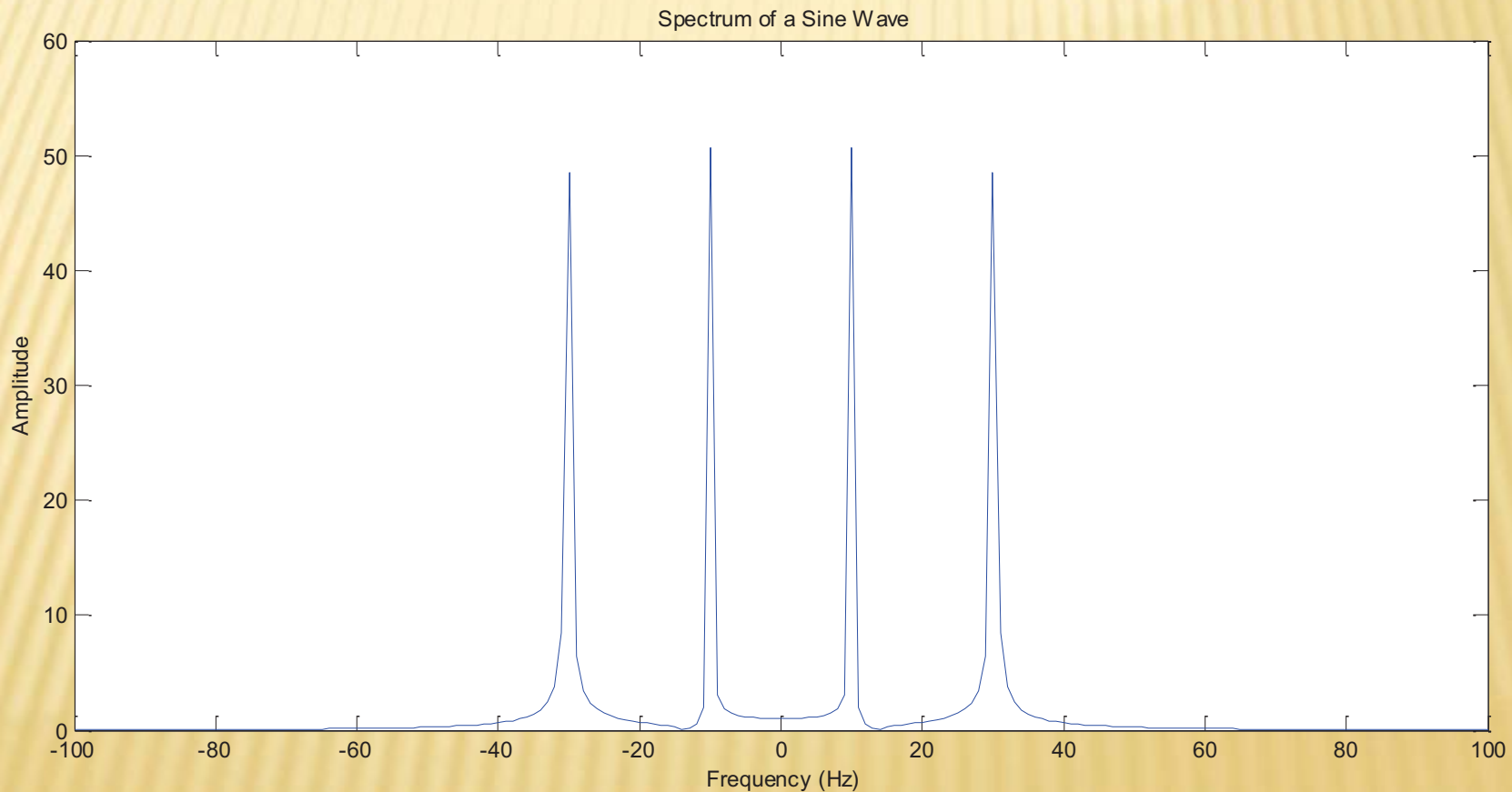


BASIC PLOTTING IN MATLAB

Example 2: Multiplication of two Cosine Waves

Plot: signal in frequency domain

$f_1 = 20$; $f_2 = 10$



BASIC PLOTTING IN MATLAB

Example 2: Multiplication of two Cosine Waves

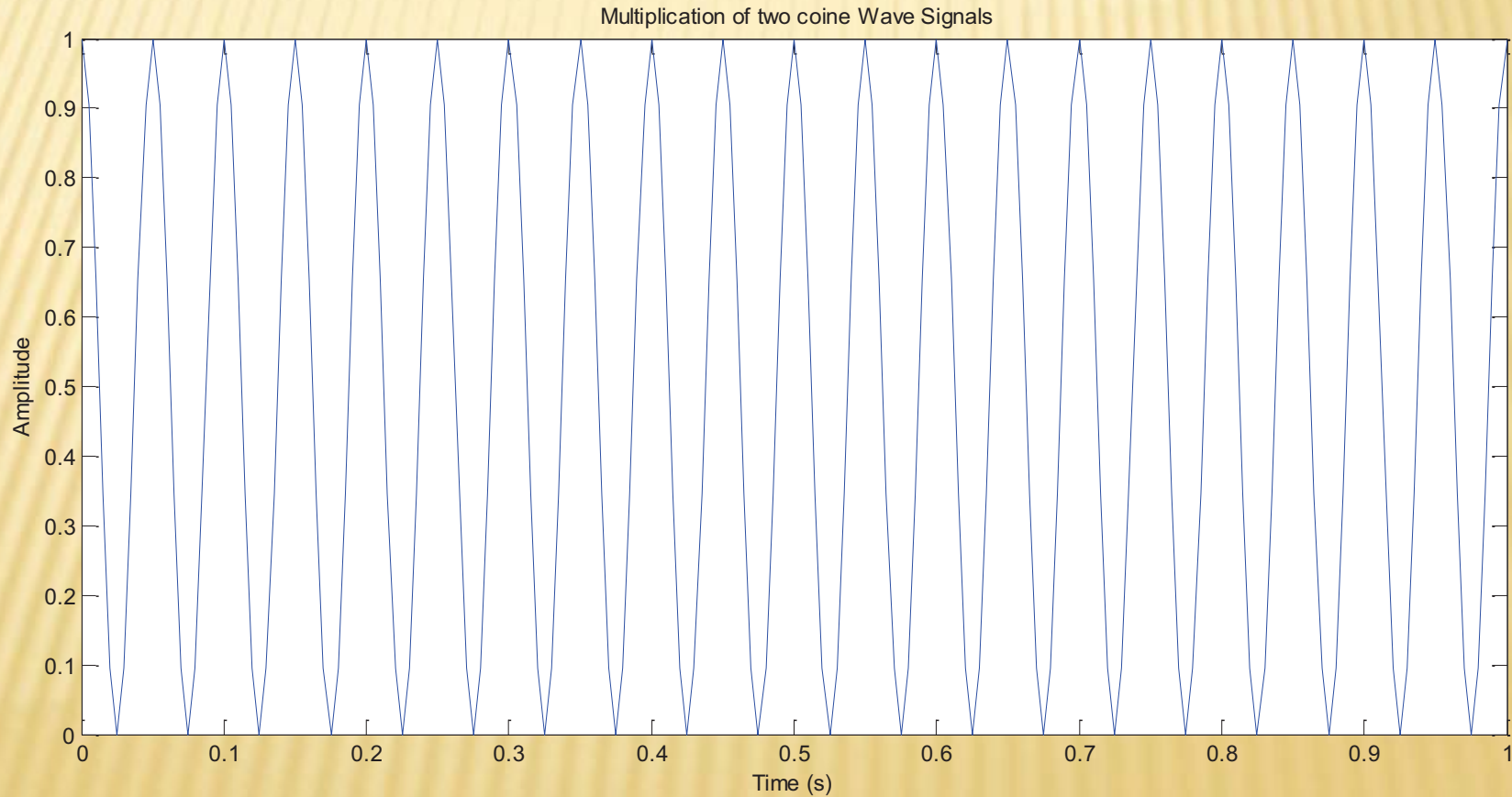
What happens when $f_1=f_2$?

BASIC PLOTTING IN MATLAB

Example 2: Multiplication of two Cosine Waves

Plot: signal in time domain

$f_1 = 10; f_2 = 10$

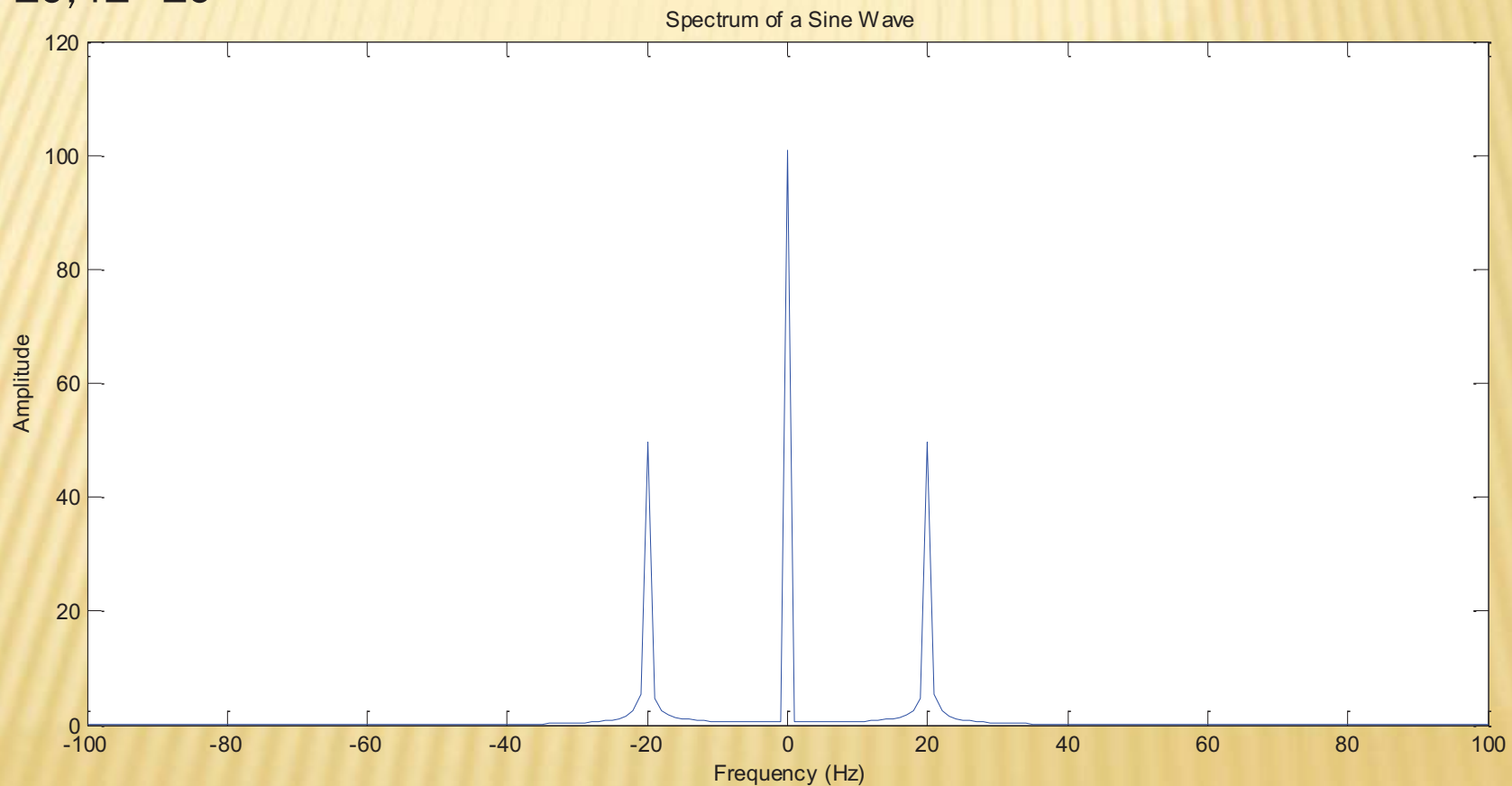


BASIC PLOTTING IN MATLAB

Example 2: Multiplication of two Cosine Waves

Plot: signal in frequency domain

$f1 = 10; f2 = 10$



It has 3 spectrum components instead of 4. Why?

BASIC PLOTTING IN MATLAB

Example 2: Multiplication of two Cosine Waves

Plot: signal in frequency domain

`f1 = 10; f2=10`

It has 3 spectrum components instead of 4. Why?

Hints:

$$\cos(2\pi f_1 t) \cdot \cos(2\pi f_2 t) = \frac{\cos(2\pi(f_1 + f_2)t) + \cos(2\pi(f_1 - f_2)t)}{2}$$

Thank You